# **Safe Learning of Lifted Action Models**







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# **1. Background and Problem Definition**

**Classical Domain Independent Planning** 

#### Given:

- A *domain* specifying the *action model of every* actions
  - An action model specifies actions' precond. and effects
- A *problem* specifying the start state and goal conditions

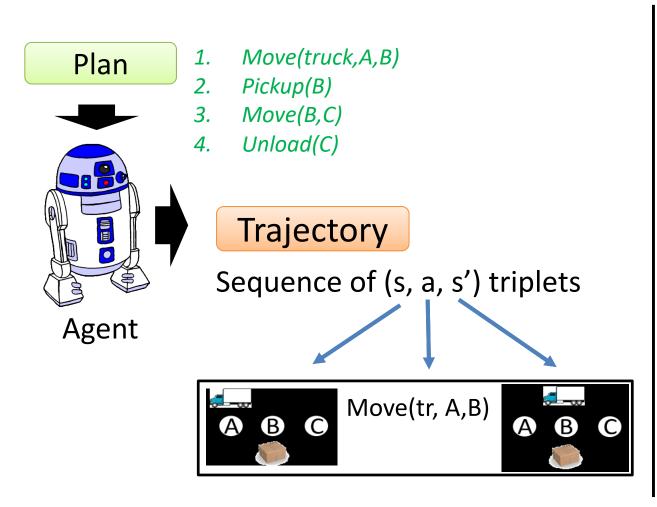
**Output:** a *plan*, i.e., sequence of actions that achieve the goal

#### **Example:** the Logistics domain



Problem can be "Package at location C" (At(Package, C))

**Execution Traces (Trajectories)** 



# Safe Model-Free Planning

#### Given:

- A *problem* **P** in some unknown domain D  $\bullet$
- A set of **trajectories** executed in D  $\bullet$ **Not given**: the real action model M\* in D

**Output:** a *plan* for P that is *sound* w.r.t M\*

Prior work: Safe Action Model (SAM) Learning [Stern & Juba '17]

- Learns a **safe action model** M<sub>safe</sub> from trajectories
- **Sound:** plans generated by M<sub>safe</sub> are sound w.r.t M\*
- **Incomplete:** M<sub>safe</sub> may be too weak to find a plan
- Does not generalize between instances of the same action

# **2. SAM Learning for Grounded Domains**

**Def**: an action model M is safe if an action A is applicable in state S iff: (1) A is applicable at S in the real action model (M\*) and (2) The effects of applying A in state S are the same for M and M\*

# Inference rules for grounded domains

Given a state-action-state triplet (s, a, s'):

- Rule 1. [Not a precondition]  $\forall l \notin s: l \notin pre(a)$
- Rule 2. [Not an effect]  $\forall l \notin s' : l \notin eff(a)$
- Rule 3. [Must be an effect]  $\forall l \in s' \setminus s: l \in eff(a)$

# SAM Learning:

1. For each action a

1.1. Initialize pre(a) to be all literals

- 1.2. Initialize eff(a) to be an empty set
- 1.3. For each state-action-triplet (s,a,s')
- 1.3.1. Apply Rule 1 to remove literals from pre(a)
- 1.3.2. Apply Rule 3 to add literals to eff(a)

# **3. Lifted Domains in Classical Planning**

A lifted domain defines

- A set of types (e.g., truck, package) and objects (truck1, package\_A)
- Lifted literals (e.g., At(x?, y?), On(x?,y?))
- Lifted actions (e.g., Move(truck?, location?, location?))

### Note: trajectories consists of grounded actions and literals

# A grounding of a literal/action is a pair (lifted literal/action, binding)

- A binding maps literal/action parameters to concrete objects
- Ex.: At(tr1, A) = (At(truck?, loc?), [truck?:tr1, loc?:A])
- Ex.: Move(tr1, A,B) = (Move(truck?, loc1?, loc2?), [truck?tr1, A:loc1?, B:loc2?])

### Preconditions and effects of lifted actions are **parameter-bound literals**

- A parameter-bound literal is a pair (lifted literal, parameters binding)
- Ex: precond. of Move(truck?,loc1?, loc2?) is (At(x?,y?), [x?: truck?, y?:loc1?]

**Def**: for a grounded action  $\langle A, b_A \rangle$  and a grounded literal  $\langle L, b_L \rangle$ , let **bindings** $(b_A, b_L)$  denote the set of all possible parameter-bindings between this action and literal, i.e.,  $\{b_{LA} | b_A \circ b_{LA} = b_L\}$ .

# **4. SAM Learning for Lifted Domains**

# **Inference rules for lifted domains**

# **5. Theoretical Properties**

Under the injective binding assumption, it holds that

Given a state-action-state triplet  $(s, (A, b_A), s')$ : Rule 1. $\forall (L, b_L) \notin s$ :  $\forall \boldsymbol{b}_{LA} \in binding(b_A, b_L): (L, b_{LA}) \notin pre(a)$ Rule 2.  $\forall (L, b_L) \notin s'$ :  $\forall \mathbf{b}_{LA} \in binding(b_A, b_L): (L, b_{LA}) \notin eff(a)$ Rule 3.  $\forall (L, b_L) \in s' \setminus s$ :  $\exists \boldsymbol{b}_{LA} \in binding(b_A, b_L): (L, b_{LA}) \in eff(a)$ 

If  $b_A$  is injective, this means  $|bindings(b_A, b_L)| = \{0,1\}$  $\rightarrow$  Rule 3 becomes simply add (L,  $b_{LA}$ ) to list of effects

- SAM learning returns the **strongest** possible **safe** action model
- Planning with the returned safe action model is **sound** but **complete** 2.
- Approximate completeness: the number of trajectories required to learn the 3. action model is linear in the size of the domain model
  - $\rightarrow$  Key: # trajectories does not depend on the number of domain objects.

**Theorem 4.** Under the injective binding assumption, given  $m \geq \frac{1}{\epsilon}(2\ln 3|\mathcal{F}||\mathcal{A}|k^d + \ln \frac{1}{\delta})$  trajectories sampled from  $\mathcal{T}_D$ , then with probability at least  $1 - \delta$  SAM learning for lifted domains (Algorithm 1) returns a safe action model  $M_{SAM}$  such that the probability of drawing from  $\mathcal{P}_D$  a problem that is not solvable with  $M_{SAM}$  is at most  $\epsilon$ .

# **6. Multiple Action Bindings**

#### What if $b_A$ is not bijective?

- **bindings** $(\boldsymbol{b}_A, \boldsymbol{b}_L)$  is a non-trivial set
- Example: consider a lifted action A(x?,y?)  $\underline{\mathsf{T1=}}\left<\{\}, A(o, o), \{L(o)\}\right>$
- <u>T2=  $\langle \{L(o_1)\}, A(o_1, o_2), \{L(o_1)\} \rangle$ </u>
- $\rightarrow$  Either L(x) is an effect or L(y) or both (Rule 3)
- $\rightarrow$  L(y) is not an effect (Rule 3)
- $\rightarrow$  L(x) is an effect!

# **7. Extended SAM Learning**

- Generate a CNF for every lifted action describing knowledge of effects
- Create proxy actions to maintain the predictability of the effects. **Example:** assume we learn for action A the following CNF:

 $\bullet$ 

#### (IsEff(L1(x)) Or IsEff(L1(y))) AND (IsEff(L2(z))) Or IsEff(L2(w)))

The generated proxy actions are::  $A_{x=y}$ : eff={L1(x)}, pre={L2(z), L2(w)}, merge x=y  $A_{z=w}$ : eff={L2(z)}, pre={L1(X), L1(Y)}, merge z=w

 $A_{x=y,z=w}$ :eff={L1(x), L2(z)}, pre={}, merge x=y, z=w

Algorithm 3: Extended SAM Learning

```
Input : \Pi_{\mathcal{T}} = \langle T, O, s_I, s_g, \mathcal{T} \rangle
    Output: (pre, eff) for a safe action model
1 \mathcal{A}' \leftarrow all lifted actions observed in \mathcal{T}
2 foreach lifted action A \in \mathcal{A}' do
         (CNF_{pre}, CNF_{eff}) \leftarrow ExtractClauses(A, \mathcal{T}(A))
        CNF_{eff}^1 \leftarrow \text{all unit clauses in } CNF_{eff}
        Surely Eff \leftarrow \{l \mid \text{IsEff}(l) \in CNF_{eff}^1\}
        SurelyPre \leftarrow \{l \mid \text{IsPre}(l) \in CN\tilde{F}_{pre}\}
         /* Create proxy actions for non-unit effects clauses *
        CNF_{eff} \leftarrow CNF_{eff} \setminus CNF_{eff}^1
         foreach S \in Powerset(\tilde{CNF}_{eff}) do
              pre(A_S) \leftarrow \text{SurelyPre}; eff(A_S) \leftarrow \text{SurelyEff}
              for each C_{eff} \in CNF_{eff} \setminus S do
                   for each IsEff(l) \in C_{eff} do
                        Add l to pre(A_S)
12
              MergeObjects(S, pre(A_S), eff(A_S))
13
14 return (pre, eff)
```

# 8. Preliminary Experimental Results

#### **9.** Summary and Future Work

- Domains: N-Puzzle (3x3 tiles, 3 predicates, 1 action), Blocksworld (8 blocks, 5 predicates, 4 actions)
- Baseline: FAMA (Aineto et al. 2019), outcome may be a unsafe

#### **Results:**

- N-Puzzle: both algorithms find the action model with a single (s,a,s') triplet.  $\bullet$
- Blocksworld: SAM learning able to find the action model with fewer trajectories

#### SAM learning can learn lifted action models!

- Number of trajectories is quasy-linear in number of lifted actions
- Does not depend on the number of objects in the world! •

**Direction for future work:** safe model-free planning in domains with continuous state variables, non-determinism, and partial observability.